

12/14/17 "What hurts more, the pain of hard work or the pain of regret?" -Unknown

HW: "Sketching Polynomials" #

Test 2 on Wednesday 12/20

AIM: How do we sketch polynomials without a graphing calculator?

Warm Up:

Given:

$$f(x) = x^6 - 5x^4 - 36x^2$$

find: (a) The complete factorization

(b) The solution set

a) $x^2(x^4 - 5x^2 - 36)$

$$x^2(x^2 - 9)(x^2 + 4)$$

$$x^2(x-3)(x+3)(x^2+4)$$

$$x=0$$

$$3$$

$$-3$$

$$\begin{array}{r} x^2 + 4 = 0 \\ -4 -4 \\ \hline 2 \\ x = -4 \end{array}$$

$$x = \pm \sqrt{-4}$$

$$x = \pm 2i$$

b) $x = 0, -3, 3, \pm 2i$

← No x term

$$x^2 = x \cdot x$$

$x \geq 0$ $x = 0$

Hw: Check

18) If 2 is a root then $x-2$ is a factor

$$\begin{array}{r}
 x^2 - 1x + 5 \\
 x-2 \overline{) x^3 - 3x^2 + 7x - 10} \\
 \underline{-(x^3 - 2x^2)} \\
 -1x^2 + 7x \\
 \underline{-(-1x^2 + 2x)} \\
 5x - 10 \\
 \underline{-(5x - 10)} \\
 0
 \end{array}$$

a) $(x-2)(x^2 - 1x + 5)$

↑ Not factorable

b) $x=2$

Use quad formula

$$x = \frac{1 \pm \sqrt{(-1)^2 - 4(1)(5)}}{2}$$

$$x = \frac{1 \pm \sqrt{-19}}{2}$$

$$x = \frac{1 \pm i\sqrt{19}}{2}$$

20) 5 is a root $x-5$ is a factor

$$\begin{array}{r}
 x^2 + 6x + 9 \\
 x-5 \overline{) x^3 + x^2 - 21x - 45} \\
 \underline{-(x^3 - 5x^2)} \\
 6x^2 - 21x \\
 \underline{-(6x^2 - 30x)} \\
 9x - 45 \\
 \underline{-(9x - 45)} \\
 0
 \end{array}$$

a) $(x-5)(x^2 + 6x + 9)$

$$(x-5)(x+3)(x+3)$$

b) $x=5, -3$

Sketching Polynomials

1) Find the zeros

2) Identify what the polynomial does @ each zero

ex: cross, touch(bounce), terrace cross

3) Identify a point on the polynomial
(\otimes y-intercept is a great one) using calculator.

4) Sketch the polynomial starting at the point from step 3

⊗ If a factor shows up once
the polynomial crosses @ that zero.

Ex: $(x+5)$ crosses @ $x=-5$

⊗ If a factor shows up an even number
times then the polynomial will touch the
x-axis @ that zero and stay on that side

Ex: $(x+5)^4$ Polynomial will touch (bounce)
@ $x=-5$

⊗ If a factor appears an odd number
of times (more than once) the polynomial
will cross @ that zero but "flatten" as it
crosses.

Ex: $(x+5)^{11}$ terrace
cross @ $x=-5$

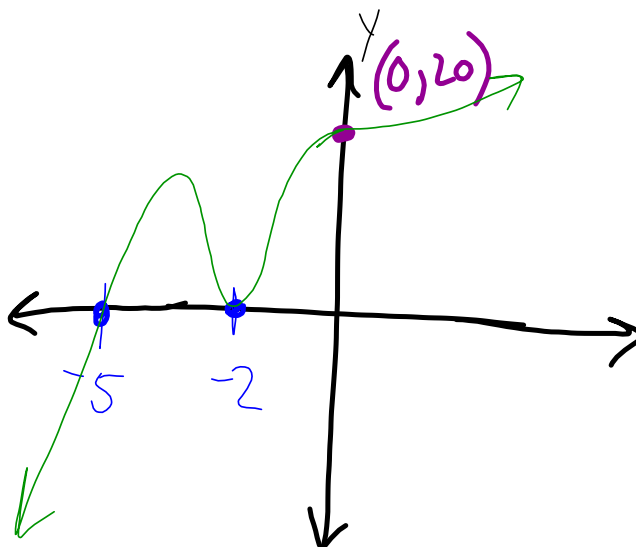
1) Sketch $P(x) = (x+2)^2 (x+5)$

$x = -2$ $x = -5$
bounce cross

⊗ x -value is
always 0 @
 y -int

$x = 0$ $y = 20$

y -int $(0, 20)$

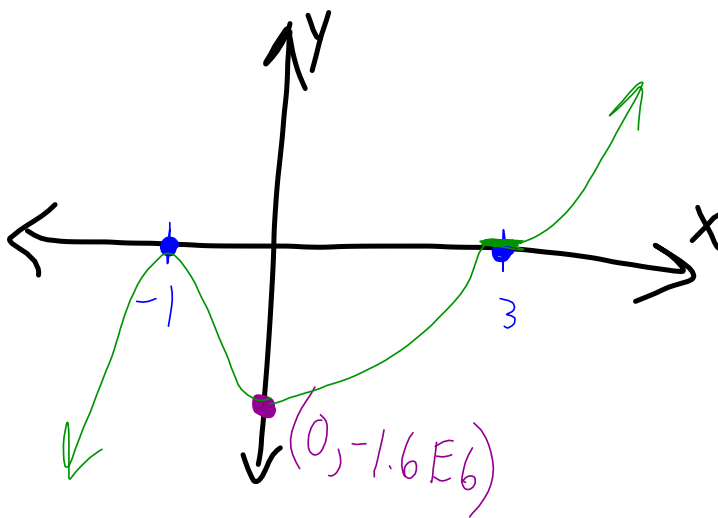


$$2) \quad P(x) = (x-3)^3 (x+1)^4$$

$x=3$ $x=-1$

terrace
cross bounce

$$y\text{-int} = (0, -1.6e^6)$$

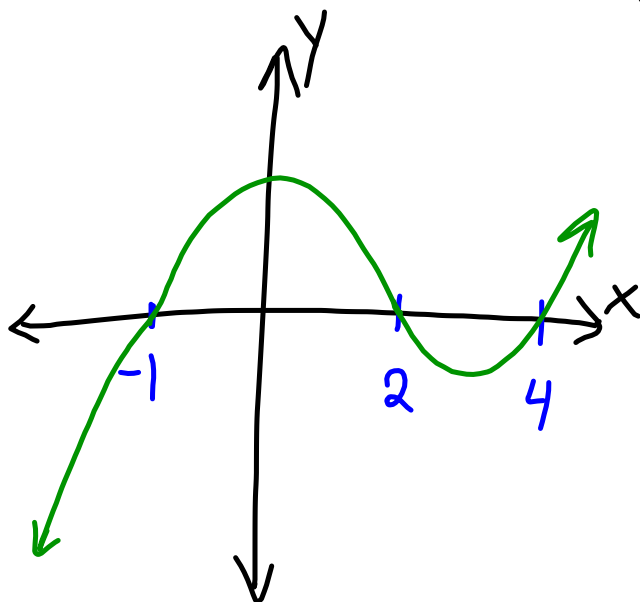


Sketch the general graph of each function without your graphing calculator. Your sketch should contain both the x - and y -intercepts.

1. $f(x) = (x+1)(x-2)(x-4)$

$x = -1, 2, 4$

	$\leftarrow \begin{array}{ c c c c } \hline \text{---} & \text{---} & \text{---} & \text{---} \\ \hline \end{array} \rightarrow$			
Test	-1	2	4	
-2		0	3	5
	$(-)(-)(-)$	$(+)(-)(-)$	$(+)(+)(-)$	$(+)(+)(+)$
	-	+	-	+



Step 1: Find the zeros

Step 2: Make a number line in order.

Step 3: Pick test values and plug them into the original. Record if it is positive or negative.

Step 4: Set up axes using the zeros as the x -intercepts. Graph the function below when Step 3 is negative and when Step 3 is positive.

2. $f(x) = -(x+3)(x+2)(x-1)$

$$f(x) = x + 3$$

$$y = x + 3$$